COMMENTS ON THE PAPER "ON THE COMBINATORIAL ANABELIAN GEOMETRY OF NODALLY NONDEGENERATE OUTER REPRESENTATIONS"

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(1.) The phrase "*of VA-type*" that appears near the beginning of Definition 2.4, (ii), should read "is *of VA-type*".

(2.) There is a slight [but substantively irrelevant] inaccuracy in the final sentence of the discussion entitled "Curves" in §0. A corrected version of this final sentence may be given as follows:

Then we shall refer to as the *n-th log configuration space* of $X^{\log}$ the log scheme obtained by pulling back the (1-)morphism $\overline{\mathcal{M}}^{\log}_{g,r+n} \to \overline{\mathcal{M}}^{\log}_{g,r}$ given by forgetting the last n points via the classifying (1-)morphism $T^{\log} \to \overline{\mathcal{M}}^{\log}_{g,r}$ of $X^{\log} \times_S T$ for some finite étale covering $T \to S$ [i.e., over which the *divisor of cusps splits*] of the underlying scheme S of $S^{\log}$ and then descending [in the evident fashion] from $T^{\log} \overset{\text{def}}{=} T \times_S S^{\log}$ to $S^{\log}$.

(3.) In the statement of Definitions 2.10, (ii); 5.1, (v), there are references to [Mzk4], Example 2.5, concerning the definition of a certain *semi-graph of anabelioids of pro-Σ PSC-type* determined by a stable log curve over a base [fs] log scheme whose underlying scheme is the spectrum of a field. At first glance, this may appear to be problematic since the "stable log curve over a base log scheme whose underlying scheme is the spectrum of a field" that appears in [Mzk4], Example 2.5, is subject to the condition that the log structure of this base log scheme be of a certain *restricted type*. In fact, this is not a problem, however, since the construction of the *semi-graph of anabelioids of pro-Σ PSC-type* in [Mzk4], Example 2.5, depends only on the *pointed stable curve* over a field determined by the given log stable curve [i.e., is *independent* of the log structure on the base log scheme].

(4.) In the second paragraph of the proof of Theorem 4.1, the text "there exists an element w'_2" should read "there exists an element $\widetilde{w}'_2$".

(5.) At the end of the second sentence of Definition 5.1, (x), the notation "$\pi_1(U_{Y_n})^{(\Sigma)}$" should read "$\pi_1(U_{Y_n})^{\Sigma}$".

(6.) In the proof of Corollary 5.3, the phrase "*graphicity* of α" should read "*graphicity* of $\alpha|_{\Pi_{2/1}}$" (2 instances); the phrase "compatibility of $\alpha_{2/1}$ with" should read "compatibility of $\alpha|_{\Pi_{2/1}}$ with" (1 instance); the notation $\alpha_{2/1}|_{\Pi_{2/1}^{\mathrm{sub}}}$ should read $\alpha|_{\Pi_{2/1}^{\mathrm{sub}}}$ (3 instances).